

# How to Get Started with DOE

With an introduction to the Design-Expert® Software\*

\*Presentation is posted at [www.statease.com/webinar.html](http://www.statease.com/webinar.html)

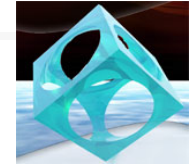
Feel free to press the raise hand 🙋 feature on GotoWebinar, which I will watch for at intervals during my presentation. To avoid disrupting the Voice over Internet Protocol (VoIP) system, I will mute all. If I do not get to you, please accept my apology in advance. Then I'd appreciate you sending me an e-mail after the talk so we can discuss your issue(s) 'off-line.' -- Brooks



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## Objective:

Show-and-tell what DOE can do with the aid of dedicated software from Stat-Ease and support of its experts.

## Agenda:

1. Introduction to DOE
  - Brief description of factorial design
  - The 4-step factorial design planning process
2. Applying the factorial design process to optimize Movie Night!—Whirley Pop™ DOE

*"Theory guides, experiment decides."*

# Real-World DOE Headlines

A very small sample\*



*John Deere Saves \$500K Annually with DOE*  
- *Scitech Journal*

*DOE Saves Kodak Thousands*  
- *Metal Forming*

*DOE Package Optimizes Coverwrap Process*  
- *Industrial Engineering Solutions*

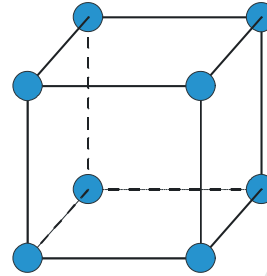
*Using DOE to Prevent Solvent Pop*  
- *Paint & Coatings Industry*

*DOE Helps Clear Wafer Transport Jams*  
- *Micro*

*DOE Attracts 3.5X More to Crayola Website*  
- *Harvard Business Review*

\*Contact [brooks@statease.com](mailto:brooks@statease.com) for these and other pubs – *likely some relevant for you.*

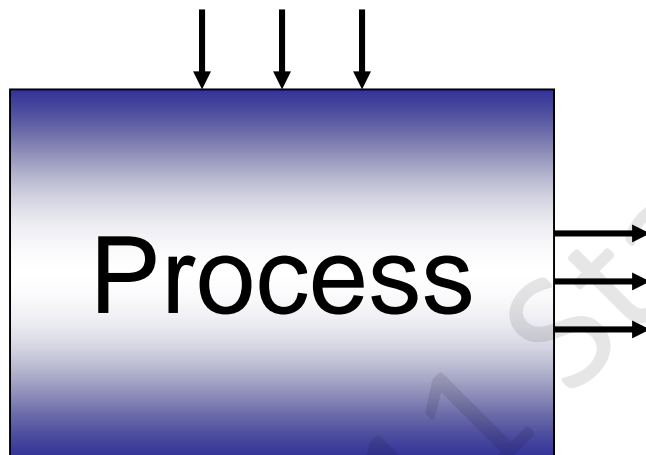
# Introduction to DOE – Factorial Designs



1. Introduction to DOE
  - Brief Description of Factorial Design
  - The 4-step factorial design planning process
2. Applying the factorial design process to optimize Movie Night!--Whirley Pop DOE

# Design of Experiments

Controllable Factors “x”



Noise Factors “z”

*Let's brainstorm.*

*What process might you experiment on for best payback? .....*

*How will you measure the response(s)*

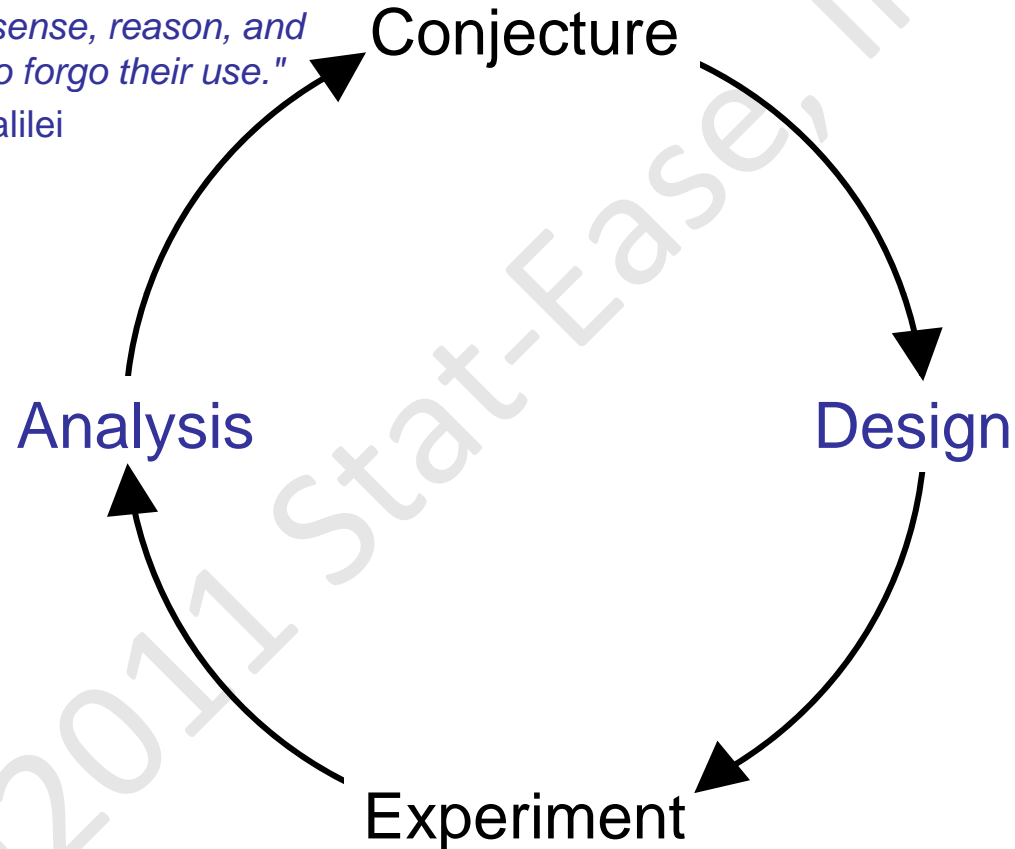
*What factors can you control?*

*Write it down.*

# Iterative Experimentation

*"I do not feel obliged to believe that the same God who has endowed us with sense, reason, and intellect has intended us to forgo their use."*

- Galileo Galilei



*Expend no more than 25% of budget on the 1st cycle.*

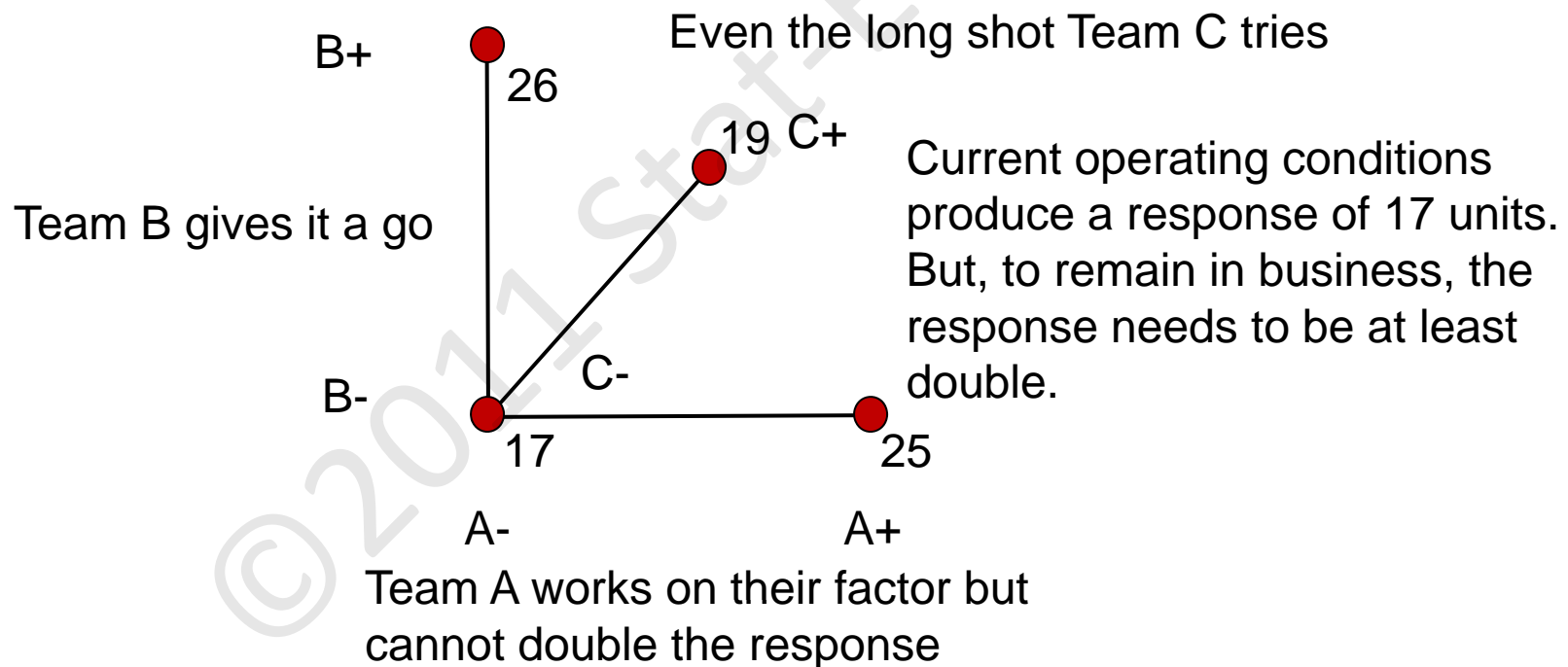
## Traditional Approach to Experimentation

- Study one factor at a time (OFAT), holding all other variables constant
- Simple process, but doesn't account for interactions
- It is inefficient (serial processing)

## Factorial Design

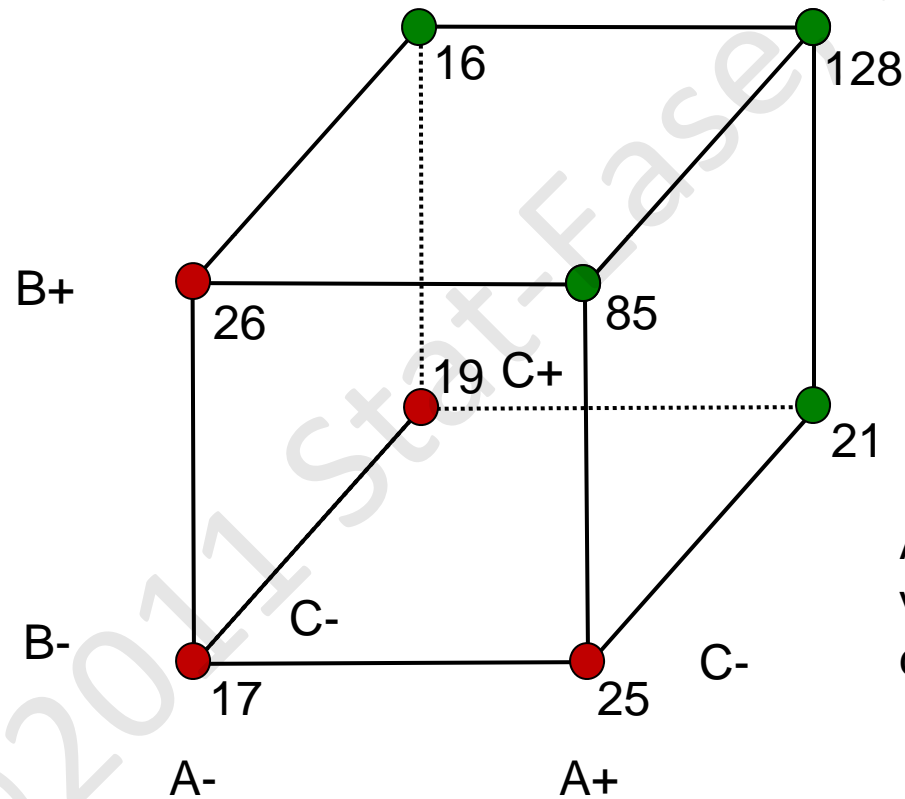
- Study multiple factors changing at once (parallel processing)
- Accounts for interactions between variables
- Maximize information with minimum runs

No meaningful improvements found with a one-factor-at-a-time experiment.



# Topic for Today

## OFAT vs. DOE



Two solutions to the problem found by uncovering the important interactions

C+

A new hire engineer volunteers to do a designed experiment

*The last example was based on a  
real occurrence at SKF.*



Ultimately SKF improved their actual bearing life from 41 million revolutions on average (already better than any competitors), to 400 million revs\* – nearly a ten-fold improvement!

\*("Breaking the Boundaries," *Design Engineering*, Feb 2000, pp 37-38.)

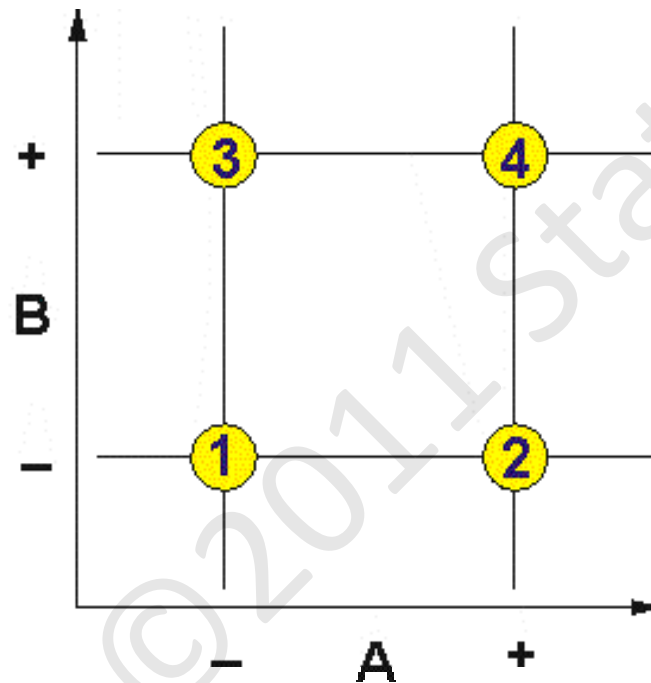
# Motivation for Factorial Design

- Want to understand how factors interact.
- Want to estimate each factor effect independent of the existence of other factor effects.
- Want to estimate factor effects well; this implies estimating effects from averages.
- Want to obtain the most information in the fewest number of runs.
- Want a **plan** to achieve goals rather than hoping to achieve goals.
- Want to keep it simple.

# Two-Level Full Factorial Design

Run all high/low combinations of 2 (or more) factors

Use statistics to identify the critical factors



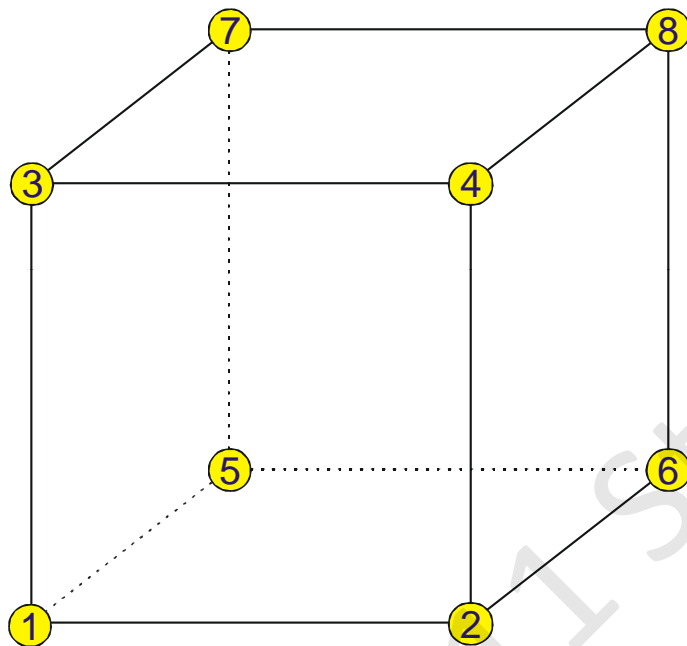
$2^2$  Full Factorial

$$\text{Effect}(\Delta y) = \frac{\sum y_+}{n_+} - \frac{\sum y_-}{n_-}$$

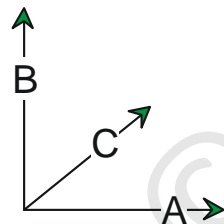
*What could be simpler?*

# Design Construction

## Independent Effect Estimates



Std	A	B	C	AB	AC	BC	ABC	
1	-	-	-	+	+	+	-	y <sub>1</sub>
2	+	-	-	-	-	+	+	y <sub>2</sub>
3	-	+	-	-	+	-	+	y <sub>3</sub>
4	+	+	-	+	-	-	-	y <sub>4</sub>
5	-	-	+	+	-	-	+	y <sub>5</sub>
6	+	-	+	-	+	-	-	y <sub>6</sub>
7	-	+	+	-	-	+	-	y <sub>7</sub>
8	+	+	+	+	+	+	+	y <sub>8</sub>



Note the pattern in each column:

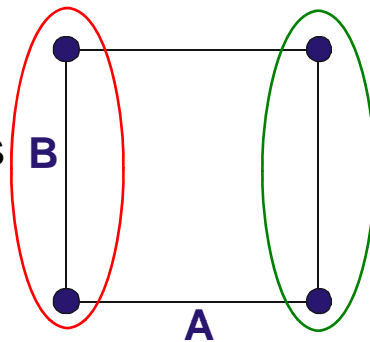
- All of the +/- patterns are unique.
- None of the patterns can be obtained by adding or subtracting any combination of the other columns
- This results in independent estimates of all the effects.

# Relative Efficiency

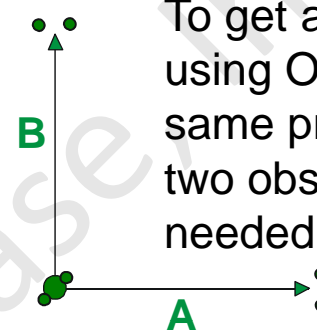
## DOE vs. OFAT

### Hidden Replication

Average observations  
 $Avg(+A) - Avg(-A)$   
 estimate the **A** effect

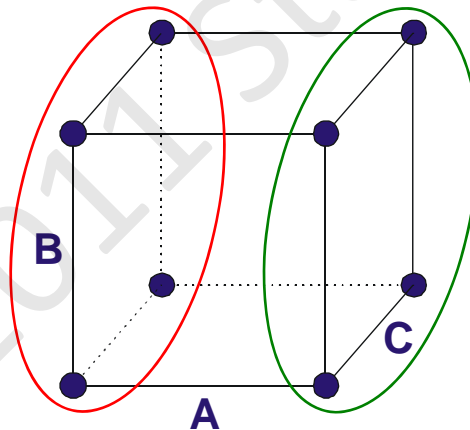


Relative efficiency =  $6/4 = 1.5$

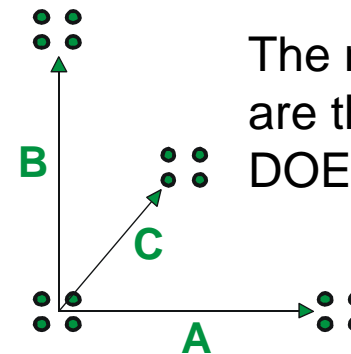


To get average estimates using OFAT that have the same precision as DOE, two observations are needed at each setting.

Hidden Replication  
 Average of four observations  
 $Avg(+A) - Avg(-A)$



Relative efficiency =  $16/8 = 2.0$



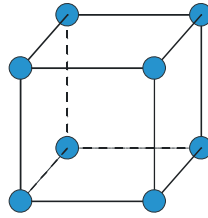
The more factors there are the more efficient DOE's become.

# Relative Efficiency

## Fractional Factorial

- All possible combinations of factors is not necessary with four or more factors.
- When budget is of primary concern...  
Fractional factorial designs (instead of full factorials) can be used with four or more factors and still provide interaction information.
  - 4 factors – 12 runs (Irregular fraction) instead of 16
  - 5 factors – 16 runs (Half-fraction) instead of 32
  - 6 factors – 22 runs (Min-Run Res V) instead of 64





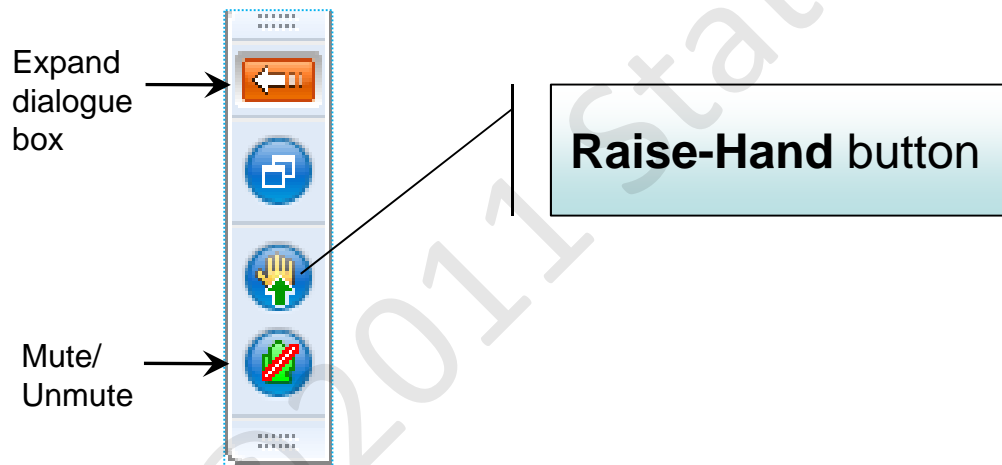
## 2<sup>k</sup> Factorial Design Advantages

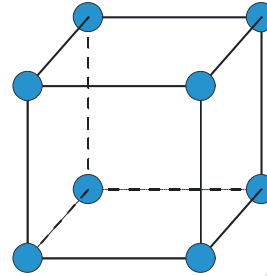
- What could be simpler?
- Minimal runs required.
  - *Can run fractions if 4 or more factors.*
- Have hidden replication.
- Wider inductive basis than OFAT experiments.
- Show interactions.
  - *Key to Success—Extremely important!*
- Easy to analyze.
- Interpretation is not difficult.
  - *Graphs make it easy.*
- Can be applied sequentially.
- Form base for more complex designs.
  - *Second order response surface design.*

# Questions?

Please Do

- Use the **Raise-Hand** button
- I will unmute your microphone so you can ask the question





1. Introduction to DOE
  - Brief description of factorial design
  - **The 4-step factorial design planning process**
2. Applying the factorial design process to optimize Movie Night!—Whirley Pop DOE

1. Identify opportunity and define objective.
2. State objective in terms of measurable responses.
  - a. Define the change ( $\Delta y$ ) that is important to detect for each response.
  - b. Estimate experimental error ( $\sigma$ ) for each response.
  - c. Use the signal-to-noise ratio ( $\Delta y/\sigma$ ) to estimate power.
3. Select the input factors to study. (*Remember that the factor levels chosen determine the size of  $\Delta y$ .*)

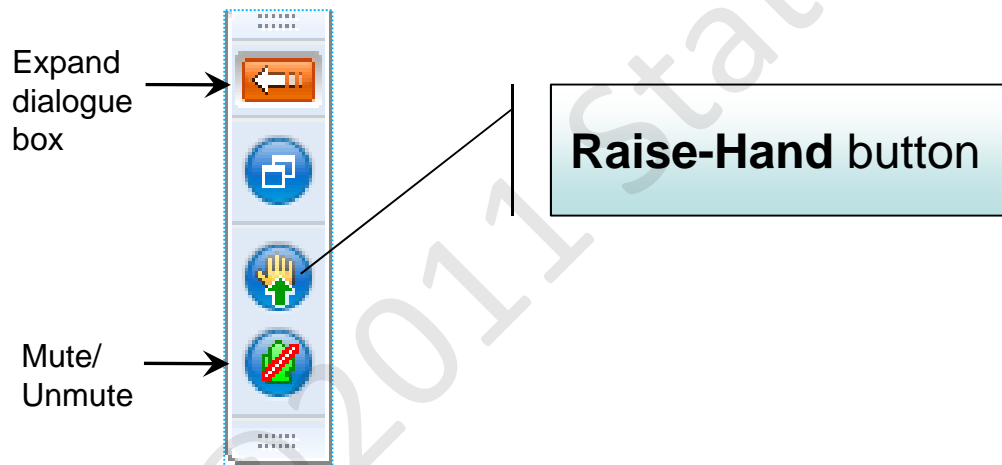
### 4. Select a design and:

- Evaluate aliases.
- Evaluate power.
- Examine the design layout to ensure all the factor combinations are safe to run and are likely to result in meaningful information (no disasters).

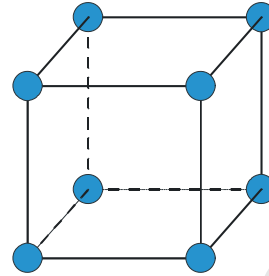
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# Agenda Transition



1. Introduction to DOE
  - Brief description of factorial design
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2. Applying the factorial design process to optimize Movie Night!—Whirley Pop DOE

# Two-Level Factorial Design

## Whirley Pop DOE

We conducted a  $2^3$  factorial design with center points. The factors are:

- A. Stirring—fraction stirred
- B. Pre-Heat Time
- C. Popcorn Type



- **Taste:** rated on a scale of 1 to 5 (best) and averaged.
  - **Texture:** rated on a scale of 1 (hard) to 5 (soft = best) and averaged.
  - **UPKs** were counted.
  - **Volume:** Estimated volume of popcorn in pot after popping
- \* For full report, see Brooks Henderson's "Whirley Pop DOE" posted at our web site: <http://www.statease.com/news/news1004.pdf>

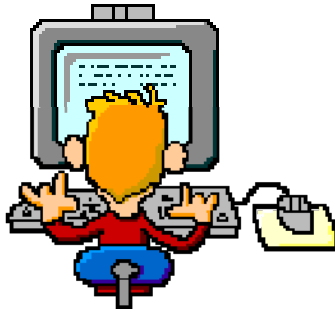
1. Identify opportunity and define objective.
  - Is stirring necessary?
  - Does Popcorn Type make a difference?
  - Determine whether to use pre-heat
2. State objective in terms of measurable responses.
  - a. Define the change ( $\Delta y$ ) that is important to detect for each response.
    - Taste:  $\pm 2$  on the rating scale of 1-5 (expect to see 3 unit change or more)
  - b. Estimate experimental error ( $\sigma$ ) for each response.
    - Taste:  $\sigma = 1$
  - c. Use the signal-to-noise ratio ( $\Delta y/\sigma$ ) to estimate power.
    - Power for 2 unit change – 68%
    - Power for 3 unit change – 95%

3. Select the input factors to study. (*Remember that the factor levels chosen determine the size of  $\Delta y$ .*)

	Name	Units	Type	Low	High
A [Numeric]	Stirring	Fraction of time	Numeric	0	1
B [Numeric]	Pre-heat	sec	Numeric	0	360
C [Categorical]	Popcorn Type	Brand	Categorical	Cheap	Costly

4. Select a design and:
- Evaluate aliases.
  - Evaluate power.
  - Examine the design layout to ensure all the factor combinations are safe to run and are likely to result in meaningful information (no disasters).

# Whirley Pop DOE Results



[Open Design-Expert Software File](#)

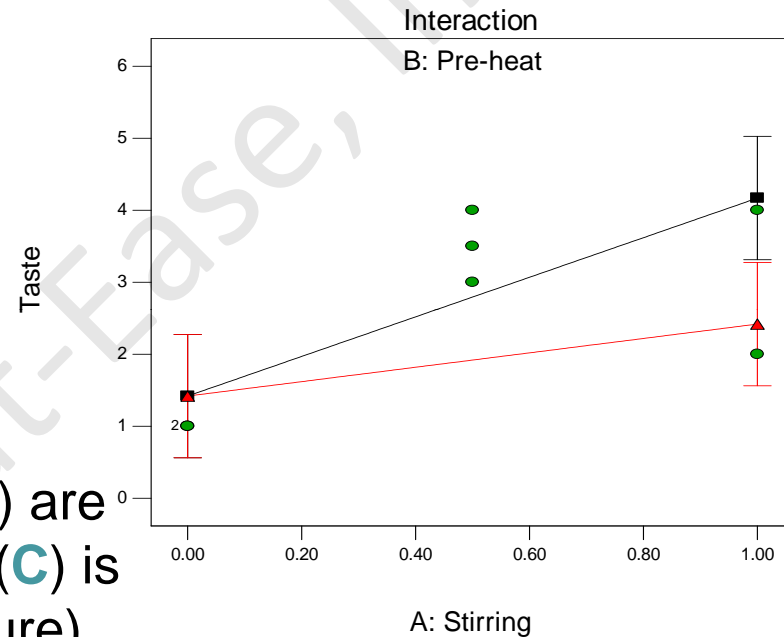
Design-Expert® Software  
Factor Coding: Actual  
Taste

● Design Points

X1 = A: Stirring  
X2 = B: Pre-heat

Actual Factor  
C: Popcorn Type = Costly

■ B- 0.00  
▲ B+ 360.00

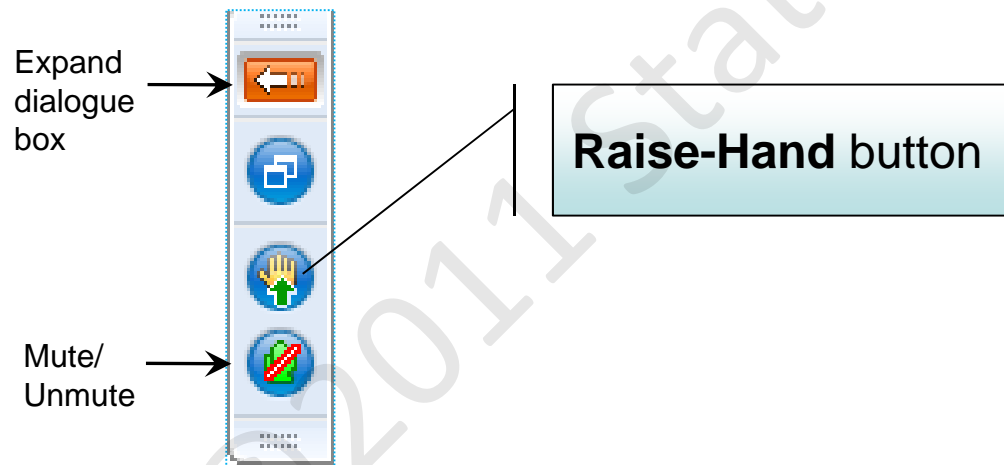


- Stirring and Preheat (**A** and **B**) are significant, but Popcorn Type (**C**) is not significant (except for texture).
  - ✓ Use constant stirring (1.0) and no preheat (0s)
  - ✓ Use Cheap popcorn to save money
- Center points indicate significant curvature. An intermediate level of stirring **MAY** give better taste and/or fewer UPKs. Augment to RSM.

# Questions?

Please Do

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- I will unmute your microphone so you can ask the question



For all the new features in v8 of Design-Expert software, see  
[www.statease.com/dx8descr.html](http://www.statease.com/dx8descr.html)



*Best of luck for your  
experimenting!*

*Thanks for listening!*

—*Brooks*

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\*Pdf of this Powerpoint presentation posted at [www.statease.com/webinar.html](http://www.statease.com/webinar.html).  
For future webinars, subscribe to DOE FAQ Alert at [www.statease.com/doesalert.html](http://www.statease.com/doesalert.html).

## How to get help




- ❑ Search publications posted at [www.statease.com](http://www.statease.com).
- ❑ In Stat-Ease software press for Screen Tips, view reports in annotated mode, look for context-sensitive Help (right-click) or search the main Help system.
- ❑ Explore Experiment Design Forum <http://forum.statease.com> and post your question (if not previously answered).
- ❑ E-mail [stathelp@statease.com](mailto:stathelp@statease.com) for answers from Stat-Ease's staff of statistical consultants.
- ❑ Call 612.378.9449 and ask for "statistical help."

- “Experiment Design Made Easy, Course Book”, Whitcomb, Kraber, Anderson, and Adams, 2011
- “Workshop: Experiment Design Made Easy,”  
<[http://www.statease.com/class\\_edme.html](http://www.statease.com/class_edme.html)>
- “I’m a beginner in design of experiments (DOE),”  
<<http://www.statease.com/beginner.html>>

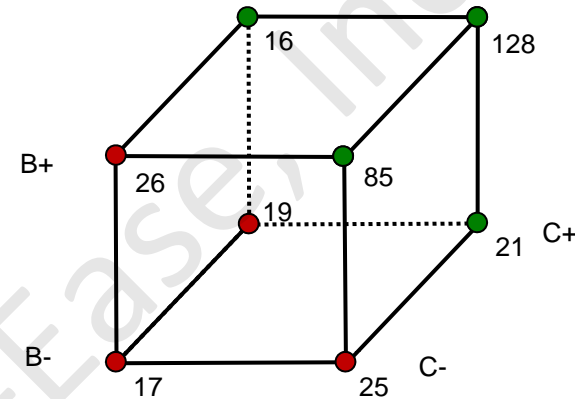
## Other References:

“Stat-Ease Webinars on Design of Experiments”,  
<<http://www.statease.com/webinar.html>>

## Appendix: Why OFAT seems to work

- OFAT approach confirmed a correct guess.
- There are only main effects active in the process.
- Sometimes it is better to be lucky. 
  - The experiment path happened to include the optimum factor combinations.
- The current operating conditions were poorly chosen.
  - Changing anything results in improvements.

# Why OFAT Fails



- There are interactions.
- The current conditions are stable but not optimal.
- The scientist guessed incorrectly and the OFAT experiment never approaches optimal settings.

## Why OFAT Fails

OFAT has problems when multiple responses relate differently to the factors.

OFAT takes more time than DOE to reach the same conclusions.

**Time is money!**